

# A Tutorial for the R Package SNPRelate

Xiuwen Zheng  
GENEVA Coordinating Center  
Department of Biostatistics  
University of Washington

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## 1 Overview

Genome-wide association studies (GWAS) are widely used to help determine the genetic basis of diseases and traits, but they pose many computational challenges. We developed gdsfmt and SNPRelate (high-performance computing R packages for multi-core symmetric

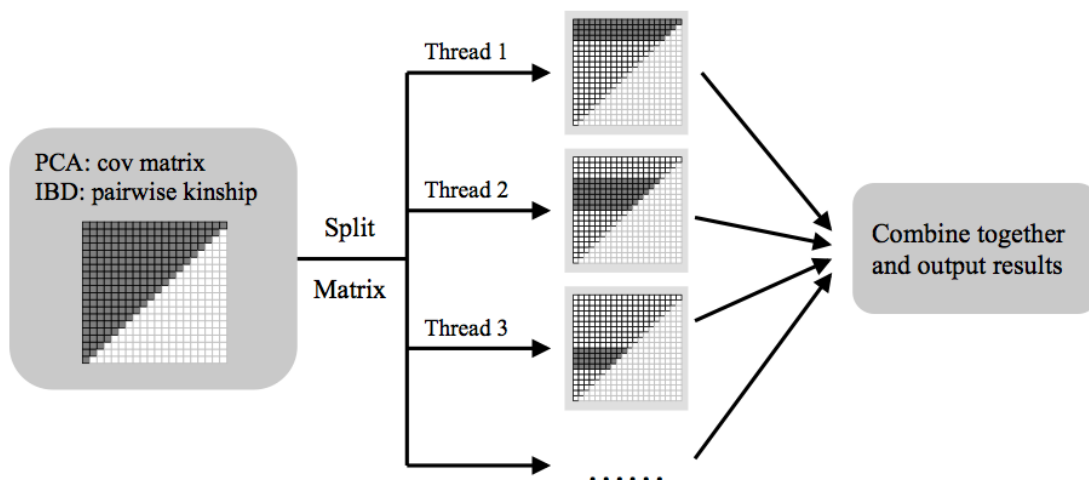


Figure 1: Flowchart of parallel computing for principal component analysis and identity-by-descent analysis.

multiprocessing computer architectures) to accelerate two key computations in GWAS: principal component analysis (PCA) and relatedness analysis using identity-by-descent (IBD) measures. The kernels of our algorithms are written in C/C++ and have been highly optimized. The calculations of the genetic covariance matrix in PCA and pairwise IBD coefficients are split into non-overlapping parts and assigned to multiple cores for performance acceleration, as shown in Figure 1. Benchmarks show the uniprocessor implementations of PCA and IBD are  $\sim 10$  to 45 times faster than the implementations provided in the popular EIGENSTRAT (v3.0) and PLINK (v1.07) programs respectively, and can be sped up to 70~250 folds by utilizing multiple cores.

R is the most popular statistical programming environment, but one not typically optimized for high performance or parallel computing which would ease the burden of large-scale GWAS calculations. To overcome these limitations we have developed a project named CoreArray (<http://corearray.sourceforge.net/>) that includes two R packages: `gdsfmt` to provide efficient, platform independent memory and file management for genome-wide numerical data, and `SNPRelate` to solve large-scale, numerically intensive GWAS calculations (i.e., PCA and IBD) on multi-core symmetric multiprocessing (SMP) computer architectures.

This vignette takes the user through the relatedness and principal component analysis used for genome wide association data. The methods in these vignettes have been introduced in the paper of Zheng *et al.* (2012).<sup>1</sup> For replication purposes the data used here are taken from the HapMap Phase II project. These data were kindly provided by the Center for Inherited Disease Research (CIDR) at Johns Hopkins University and the Broad Institute of MIT and Harvard University (Broad). The data supplied here should not be used for any purpose other than this tutorial.

<sup>1</sup>Zheng, Xiuwen., *et al.* A High-performance Computing Toolset for Relatedness and Principal Component Analysis in GWAS. *Submitted*.

## 2 Preparing Data

### 2.1 Data formats used in SNPRelate

To support efficient memory management for genome-wide numerical data, the `gdsfmt` package provides the genomic data structure (GDS) file format for array-oriented bioinformatic data, which is a container for storing annotation data and SNP genotypes. In this format each byte encodes up to four SNP genotypes thereby reducing file size and access time. The GDS format supports data blocking so that only the subset of data that is being processed needs to reside in memory. GDS formatted data is also designed for efficient random access to large data sets.

```
> # load the R packages: gdsfmt and SNPRelate
> library(gdsfmt)
> library(SNPRelate)
```

Here is a typical GDS file:

```
> snpgdsSummary(snpGdsExampleFileName())
```

The total number of samples: 279

The total number of SNPs: 9088

SNP genotypes are stored in individual-major mode.

`snpGdsExampleFileName()` returns the file name of a GDS file used as an example in `SNPRelate`, and it is a subset of data from the HapMap project and the samples were genotyped by the Center for Inherited Disease Research (CIDR) at Johns Hopkins University and the Broad Institute of MIT and Harvard University (Broad). `snpGdsSummary()` summarizes the genotypes stored in the GDS file. “Individual-major mode” indicates listing all SNPs for an individual before listing the SNPs for the next individual, etc. Conversely, “SNP-major mode” indicates listing all individuals for the first SNP before listing all individuals for the second SNP, etc. Sometimes “SNP-major mode” is more computationally efficient than “individual-major mode”. For example, the calculation of genetic covariance matrix deals with genotypic data SNP by SNP, and then “SNP-major mode” should be more efficient.

```
> # open a GDS file
> (genofile <- openfn.gds(snpGdsExampleFileName()))
```

file name: /Library/Frameworks/R.framework/Versions/2.15/Resources/library/SNPRelate/ext

```
+      [  ]
|--- sample.id      [ FStr8 279 ZIP(23.10%) ]
|--- snp.id         [ Int32 9088 ZIP(34.76%) ]
|--- snp.rs.id      [ FStr8 9088 ZIP(42.66%) ]
```

```

|--+ snp.position      [ Float64 9088 ZIP(51.77%) ]
|--+ snp.chromosome    [ Int32 9088 ZIP(0.33%) ]
|--+ snp.allele        [ FStr8 9088 ZIP(14.45%) ]
|--+ genotype         [ Bit2 9088x279 ]
|--+ sample.annot      [   ] *
| |--+ sample.id       [ FStr8 279 ZIP(23.10%) ]
| |--+ family.id       [ FStr8 279 ZIP(28.37%) ]
| |--+ geneva.id       [ Int32 279 ZIP(80.29%) ]
| |--+ father.id       [ FStr8 279 ZIP(12.98%) ]
| |--+ mother.id       [ FStr8 279 ZIP(12.86%) ]
| |--+ plate.id        [ FStr8 279 ZIP(1.29%) ]
| |--+ sex             [ FStr8 279 ZIP(28.32%) ]
| |--+ pop.group       [ FStr8 279 ZIP(7.89%) ]

```

The output lists all variables stored in the GDS file. At the first level, it saves variables **sample.id**, **snp.id**, etc. The second-level variables **sex** and **pop.group** are both stored in the directory of **sample.annot**. All of the functions in **SNPRelate** require a minimum set of variables in the SNP annotation data. The minimum required variables are

- **snp.id**, a unique identifier for each SNP;
- **snp.chromosome**, an integer mapping for each chromosome, with values 1-26, mapped in order from 1-22, 23=X, 24=XY (the pseudoautosomal region), 25=Y, 26=M (the mitochondrial probes), and 0 for probes with unknown positions; it does not allow NA.
- **snp.position**, the base position of each SNP on the chromosome, and 0 for unknown position; it does not allow NA.

```

> # Take out snp.id
> head(read.gdsn(index.gdsn(genofile, "snp.id")))

[1] 1 2 3 4 5 6

> # Take out snp.rs.id
> head(read.gdsn(index.gdsn(genofile, "snp.rs.id")))

[1] "rs1695824" "rs13328662" "rs4654497" "rs10915489" "rs12132314"
[6] "rs12042555"

```

There are two additional variables:

- **snp.rs.id**, a character string identifier for the SNP that may not be unique.
- **snp.allele**, it is not necessary for the analysis, but it is necessary when merging genotypes from different platforms. The format of **snp.allele** is “A allele/B allele”, like “T/G” where T is A allele and G is B allele.

There are four possible values stored in the variable **genotype**: 0, 1, 2 and 3. “0” indicates two B alleles, “1” indicates one A allele and one B allele, “2” indicates two A alleles, and “3” is a missing genotype. “Bit2” indicates that each byte encodes up to four SNP genotypes since one byte consists of eight bits.

```
> # Take out genotype data for the first 3 samples and the first 5 SNPs
> (g <- read.gdsn(index.gdsn(genofile, "genotype"), start=c(1,1), count=c(5,3)))

      [,1] [,2] [,3]
[1,]    2    1    2
[2,]    1    1    1
[3,]    0    0    1
[4,]    1    1    2
[5,]    2    2    2

> # read population information
> pop <- read.gdsn(index.gdsn(genofile, c("sample.annot", "pop.group")))
> table(pop)

pop
CEU HCB JPT YRI
 92  47  47  93

> # close the GDS file
> closefn.gds(genofile)
```

## 2.2 Create a GDS File of Your Own

The function **snpgdsCreateGeno** helps to create a GDS file of your own. There are possible values stored in the input genotype matrix: 0, 1, 2 and other values. “0” indicates two B alleles, “1” indicates one A allele and one B allele, “2” indicates two A alleles, and other values indicate a missing genotype. For example,

```
> # load data
> data(hapmap.geno)
> # create a gds file
> with(hapmap.geno, snpgdsCreateGeno("test.gds", genmat=genotype,
+   sample.id=sample.id, snp.id=snp.id, snp.chromosome=snp.chromosome,
+   snp.position=snp.position, snp.allele=snp.allele, snp.firstorder=TRUE))
> # open the gds file
> (genofile <- openfn.gds("test.gds"))

file name: test.gds
```

```

+          [      ]
|---+ sample.id          [ FStr8 279 ZIP(23.10%) ]
|---+ snp.id             [ FStr8 1000 ZIP(45.02%) ]
|---+ snp.position       [ Float64 1000 ZIP(55.97%) ]
|---+ snp.chromosome     [ Int32 1000 ZIP(2.00%) ]
|---+ snp.allele        [ FStr8 1000 ZIP(17.37%) ]
|---+ genotype          [ Bit2 1000x279 ] *

> # close the genotype file
> closefn.gds(genofile)

```

## 2.3 Format conversion from PLINK binary files

The SNPRelate package provides a function `snpgdsBED2GDS` for converting a PLINK binary file to a GDS file:

```

> # the PLINK BED file
> bed.fn <- system.file("extdata", "plinkhapmap.bed", package="SNPRelate")
> bim.fn <- system.file("extdata", "plinkhapmap.bim", package="SNPRelate")
> fam.fn <- system.file("extdata", "plinkhapmap.fam", package="SNPRelate")
> # convert
> snpgdsBED2GDS(bed.fn, fam.fn, bim.fn, "test.gds")

```

Start `snpgdsBED2GDS` ...

```

      open /Library/Frameworks/R.framework/Versions/2.15/Resources/library/SNPRelate/e
      open /Library/Frameworks/R.framework/Versions/2.15/Resources/library/SNPRelate/e
      open /Library/Frameworks/R.framework/Versions/2.15/Resources/library/SNPRelate/e
Fri Jul 20 04:48:08 2012      store sample id, snp id, position, and chromosome.
      start writing ...
      Fri Jul 20 04:48:08 2012      0%
      Fri Jul 20 04:48:08 2012      100%
Fri Jul 20 04:48:08 2012      Done.

```

```

> # summary
> snpgdsSummary("test.gds")

```

The total number of samples: 279

The total number of SNPs: 5000

SNP genotypes are stored in individual-major mode.

## 2.4 Format conversion from Sequence VCF files

The SNPRelate package provides a function `snpgdsVCF2GDS` for converting a VCF file to a GDS file:

```

> # the VCF file
> vcf.fn <- system.file("extdata", "sequence.vcf", package="SNPRelate")
> # convert
> snpgdsVCF2GDS(vcf.fn, "test.gds")

Start snpgdsVCF2GDS ...
      Open /Library/Frameworks/R.framework/Versions/2.15/Resources/library/SNPRelate/e
      Scanning ...
Fri Jul 20 04:48:09 2012      store sample id, snp id, position, and chromosome.
      start writing ...
Fri Jul 20 04:48:09 2012      Done.

> # summary
> snpgdsSummary("test.gds")

The total number of samples: 3
The total number of SNPs: 2
SNP genotypes are stored in SNP-major mode.

```

### 3 Data Analysis

We developed `gdsfmt` and `SNPRelate` (high-performance computing R packages for multi-core symmetric multiprocessing computer architectures) to accelerate two key computations in GWAS: principal component analysis (PCA) and relatedness analysis using identity-by-descent (IBD) measures.

```

> # open the GDS file
> genofile <- openfn.gds(snpGdsExampleFileName())

```

#### 3.1 LD-based SNP pruning

It is important to use a pruned set of SNPs which are in approximate linkage equilibrium with each other to avoid the strong influence of SNP clusters in principal component analysis and relatedness analysis.

```

> set.seed(1000)
> # try different LD thresholds for sensitivity analysis
> snpset <- snpgdsLDpruning(genofile, ld.threshold=0.2)

```

SNP pruning based on LD:

```

      Sliding window: 500000 basepairs, Inf SNPs
      |LD| threshold: 0.2
Removing 365 non-autosomal SNPs

```

Removing 1 SNPs (monomorphic, < MAF, or > missing rate)

Working space: 279 samples, 8722 SNPs

Chromosome 1: 75.42%, 540/716

Chromosome 2: 72.24%, 536/742

Chromosome 3: 74.71%, 455/609

Chromosome 4: 73.31%, 412/562

Chromosome 5: 77.03%, 436/566

Chromosome 6: 75.58%, 427/565

Chromosome 7: 75.42%, 356/472

Chromosome 8: 71.31%, 348/488

Chromosome 9: 77.88%, 324/416

Chromosome 10: 74.33%, 359/483

Chromosome 11: 77.40%, 346/447

Chromosome 12: 76.81%, 328/427

Chromosome 13: 75.58%, 260/344

Chromosome 14: 76.95%, 217/282

Chromosome 15: 76.34%, 200/262

Chromosome 16: 72.66%, 202/278

Chromosome 17: 74.40%, 154/207

Chromosome 18: 73.68%, 196/266

Chromosome 19: 85.00%, 102/120

Chromosome 20: 71.62%, 164/229

Chromosome 21: 76.98%, 97/126

Chromosome 22: 75.86%, 88/116

6547 SNPs are selected in total.

```
> names(snpset)
```

```
[1] "chr1" "chr2" "chr3" "chr4" "chr5" "chr6" "chr7" "chr8" "chr9"
[10] "chr10" "chr11" "chr12" "chr13" "chr14" "chr15" "chr16" "chr17" "chr18"
[19] "chr19" "chr20" "chr21" "chr22"
```

```
> head(snpset$chr1) # snp.id
```

```
[1] 1 2 4 5 7 10
```

```
> # get all selected snp id
```

```
> snpset.id <- unlist(snpset)
```

## 3.2 Principal Component Analysis

The functions in **SNPRelate** for PCA include calculating the genetic covariance matrix from genotypes, computing the correlation coefficients between sample loadings and genotypes for each SNP, calculating SNP eigenvectors (loadings), and estimating the sample loadings of a new dataset from specified SNP eigenvectors.

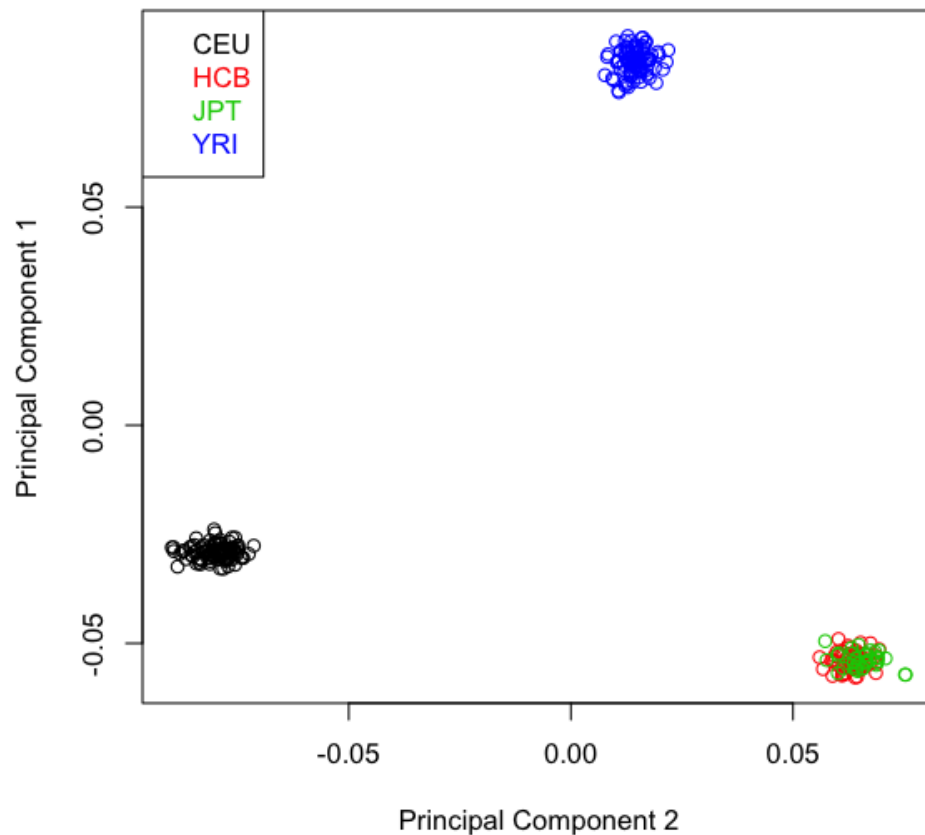
```

> pca <- snpgdsPCA(genofile, maf=0.05, missing.rate=0.05,
+               snp.id=snpset.id, num.thread=2)

Principal Component Analysis (PCA) on SNP genotypes:
Removing 1112 SNPs (monomorphic, < MAF, or > missing rate)
Working space: 279 samples, 5435 SNPs
      Using 2 CPU cores.
PCA:      the sum of all working genotypes = 1520750
PCA:      Fri Jul 20 04:48:10 2012      0%
PCA:      Fri Jul 20 04:48:10 2012      100%
PCA:      Fri Jul 20 04:48:10 2012      Begin (eigenvalues and eigenvectors)
PCA:      Fri Jul 20 04:48:10 2012      End (eigenvalues and eigenvectors)

> plot(pca$eigenvect[,2], pca$eigenvect[,1], xlab="Principal Component 2",
+      ylab="Principal Component 1", type="n")
> # uses different colors with respect to ethnicities
> race <- as.factor(read.gdsn(index.gdsn(genofile,
+      c("sample.annot", "pop.group"))))
> points(pca$eigenvect[,2], pca$eigenvect[,1], col=race)
> legend("topleft", legend=levels(race), text.col=1:nlevels(race))

```



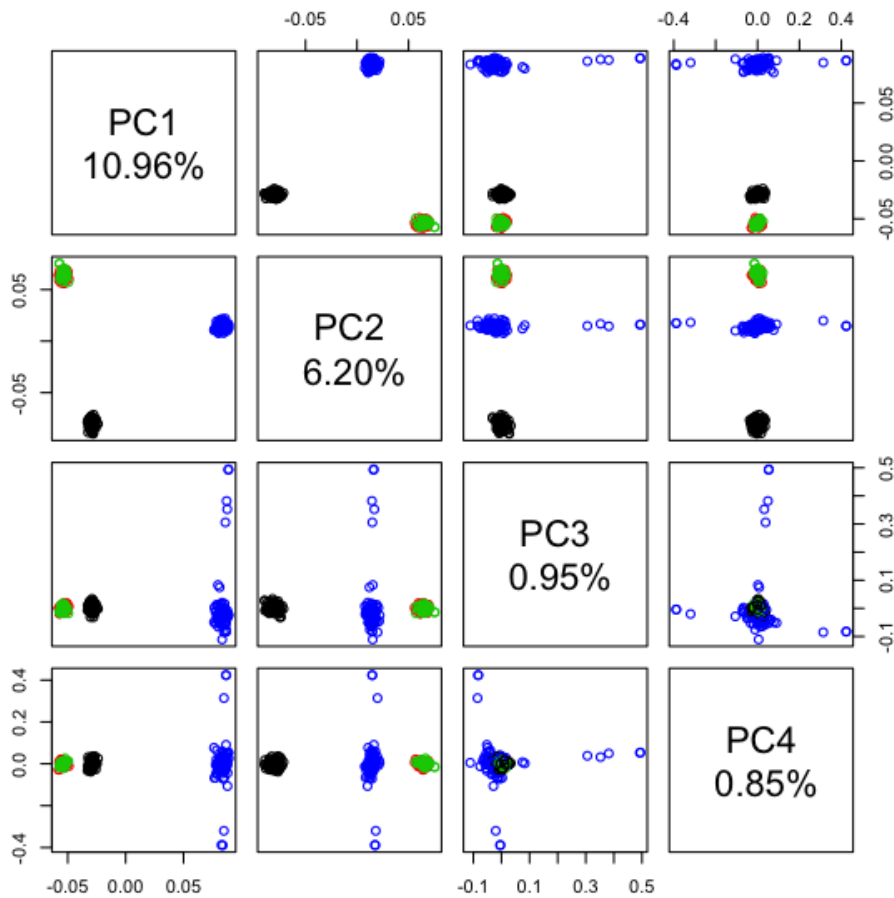
The code below shows how to calculate the percent of variation is accounted for by the principal component for the first 16 PCs. It is clear to see the first two eigenvectors hold the largest percentage of variance among the population, although the total variance accounted for is still less the one-quarter of the total.

```
> pc.percent <- 100 * pca$eigenval[1:16]/sum(pca$eigenval)
> pc.percent

[1] 10.9608123  6.1973872  0.9480086  0.8526434  0.7927158  0.7804631
[7]  0.7496657  0.7139979  0.6759434  0.6680874  0.6605878  0.6591129
[13]  0.6501947  0.6441370  0.6372978  0.6281596
```

Plot the principal component pairs for the first four PCs:

```
> lbls <- paste("PC", 1:4, "\n", format(pc.percent[1:4], digits=2), "%", sep="")
> pairs(pca$eigenvect[,1:4], col=race, labels=lbls)
```



To calculate the SNP correlations between eigenvectors and SNP genotypes:

```
> # get chromosome index
> chr <- read.gdsn(index.gdsn(genofile, "snp.chromosome"))
> CORR <- snpgdsPCACorr(pca, genofile, eig.which=1:4)
```

SNP correlations:

Working space: 279 samples, 9088 SNPs

Using 1 CPU core.

Using the top 32 eigenvectors.

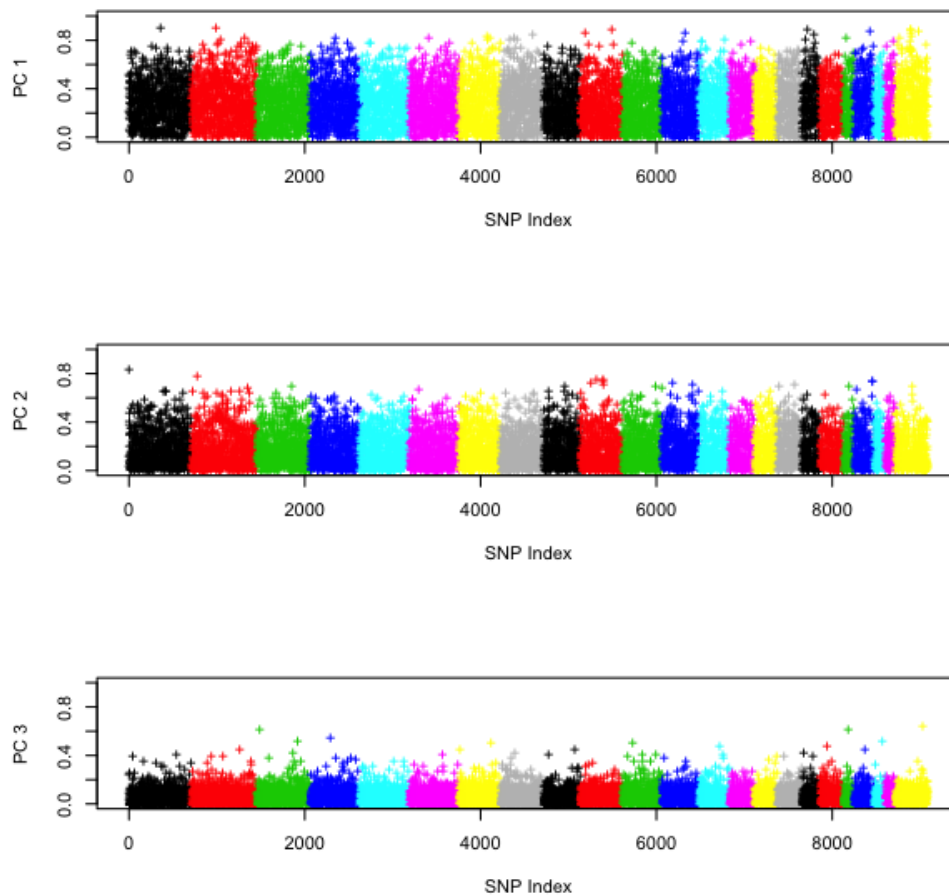
SNP Correlations: the sum of all working genotypes = 2553065

SNP Correlations: Fri Jul 20 04:48:11 2012 0%

SNP Correlations: Fri Jul 20 04:48:11 2012 100%

```
> par( mfrow=c(3,1))
> for (i in 1:3)
+ {
```

```
+      plot(abs(CORR$snpcorr[i,]), ylim=c(0,1), xlab="SNP Index",
+           ylab=paste("PC", i), col=chr, pch="+")
+ }
```



### 3.3 Relatedness Analysis

For relatedness analysis, identity-by-descent (IBD) estimation in **SNPRelate** can be done by either the method of moments (MoM) (Purcell et al., 2007) or maximum likelihood estimation (MLE) (Milligan, 2003; Choi et al., 2009). Although MLE estimates are more reliable than MoM, MLE is significantly more computationally intensive. For both of these methods it is preferred to use a LD pruned SNP set.

```
> # YRI samples
> sample.id <- read.gdsn(index.gdsn(genofile, "sample.id"))
> YRI.id <- sample.id[read.gdsn(index.gdsn(genofile,
+      c("sample.annot", "pop.group"))) == "YRI"]
```

### 3.3.1 PLINK method of moments (MoM)

```
> # estimate IBD coefficients
> ibd <- snpgdsIBDMoM(genofile, sample.id=YRI.id, snp.id=snpset.id,
+ maf=0.05, missing.rate=0.05)
```

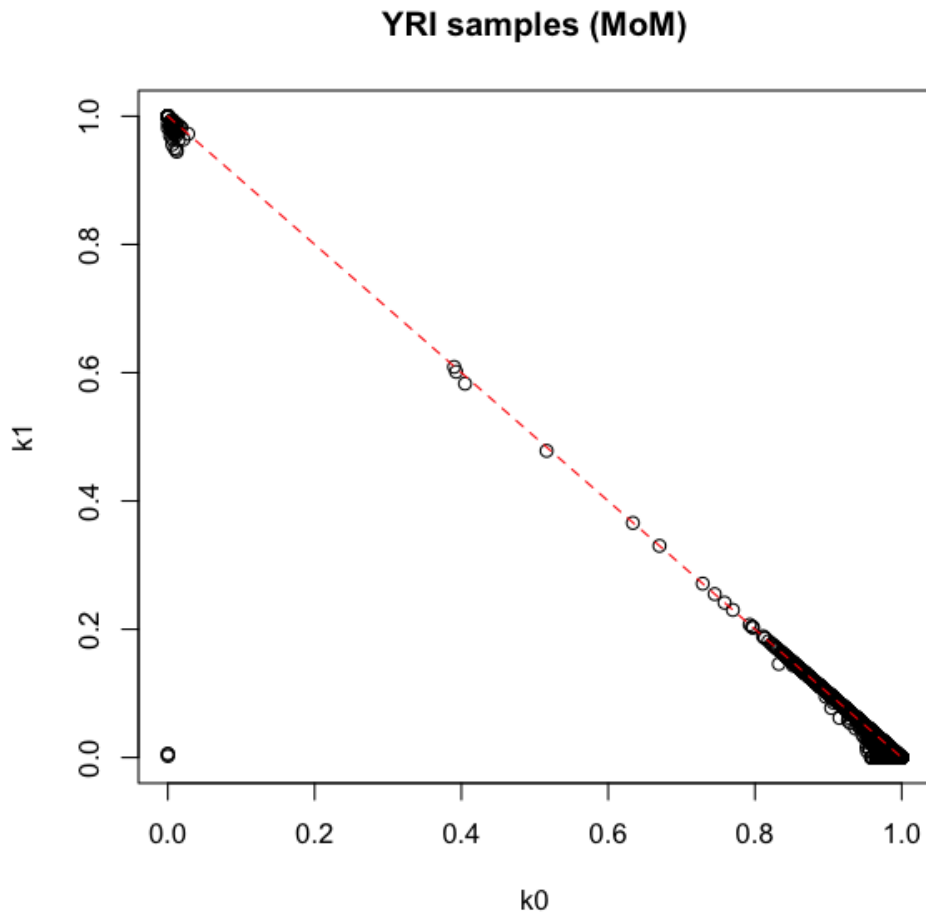
Identity-By-Descent analysis (PLINK method of moment) on SNP genotypes:  
Removing 1285 SNPs (monomorphic, < MAF, or > missing rate)  
Working space: 93 samples, 5262 SNPs  
Using 1 CPU core.

```
PLINK IBD:      the sum of all working genotypes = 484520
PLINK IBD:      Fri Jul 20 04:49:20 2012      0%
PLINK IBD:      Fri Jul 20 04:49:20 2012      100%
```

```
> ibd.coeff <- snpgdsIBDSelection(ibd)
> head(ibd.coeff)
```

	sample1	sample2	k0	k1	kinshipcoeff
1	NA19152	NA19139	0.9548539	0.04514610	0.011286524
2	NA19152	NA18912	1.0000000	0.00000000	0.000000000
3	NA19152	NA19160	1.0000000	0.00000000	0.000000000
4	NA19152	NA18515	0.9234541	0.07654590	0.019136475
5	NA19152	NA19222	1.0000000	0.00000000	0.000000000
6	NA19152	NA18508	0.9833803	0.01661969	0.004154922

```
> plot(ibd.coeff$k0, ibd.coeff$k1, xlim=c(0,1), ylim=c(0,1),
+ xlab="k0", ylab="k1", main="YRI samples (MoM)")
> lines(c(0,1), c(1,0), col="red", lty=2)
```



### 3.3.2 IBD Using Maximum Likelihood Estimation (MLE)

```
> # estimate IBD coefficients
> set.seed(1000)
> snp.id <- sample(snpset.id, 5000) # random 5000 SNPs
> ibd <- snpgdsIBDMLE(genofile, sample.id=YRI.id, snp.id=snp.id,
+ maf=0.05, missing.rate=0.05)
```

Identity-By-Descent analysis (MLE) on SNP genotypes:  
 Removing 981 SNPs (monomorphic, < MAF, or > missing rate)  
 Working space: 93 samples, 4019 SNPs  
 Using 1 CPU core.

```
MLE IBD:      the sum of all working genotypes = 369973
MLE IBD:      Fri Jul 20 04:49:21 2012      0%
MLE IBD:      Fri Jul 20 04:49:45 2012      6%
MLE IBD:      Fri Jul 20 04:50:08 2012     12%
```

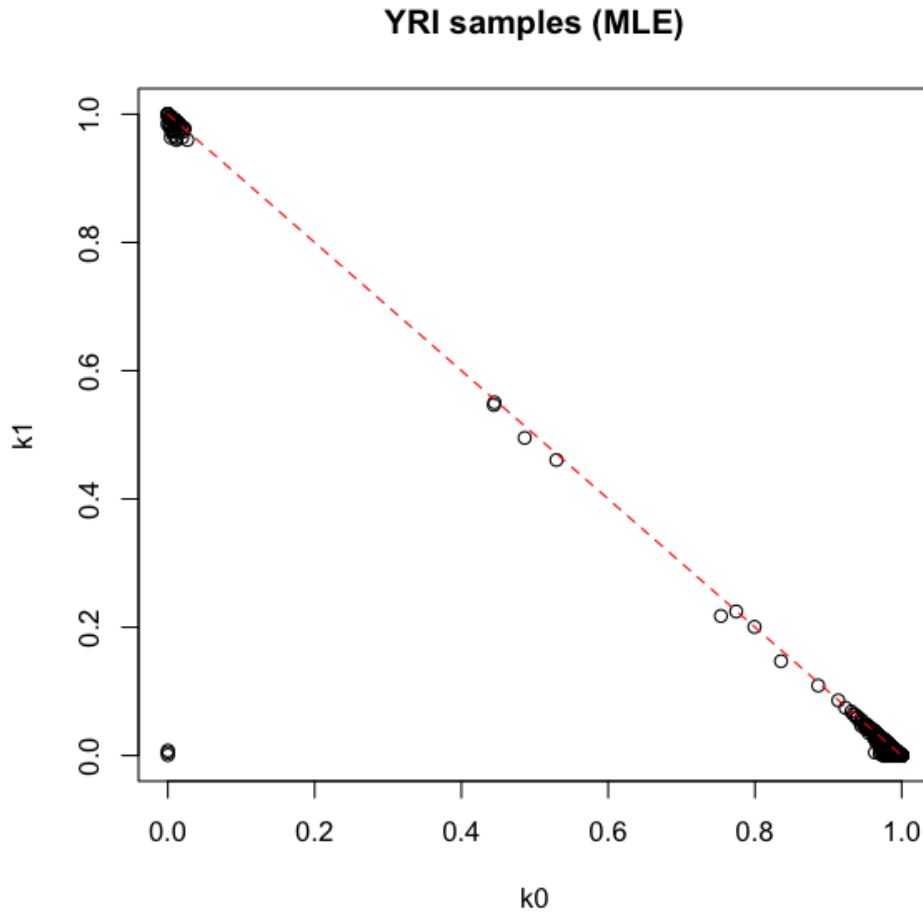
MLE IBD:	Fri Jul 20 04:50:29 2012	19%
MLE IBD:	Fri Jul 20 04:50:57 2012	26%
MLE IBD:	Fri Jul 20 04:51:19 2012	32%
MLE IBD:	Fri Jul 20 04:51:42 2012	38%
MLE IBD:	Fri Jul 20 04:52:11 2012	45%
MLE IBD:	Fri Jul 20 04:52:41 2012	51%
MLE IBD:	Fri Jul 20 04:53:09 2012	57%
MLE IBD:	Fri Jul 20 04:53:35 2012	64%
MLE IBD:	Fri Jul 20 04:54:02 2012	70%
MLE IBD:	Fri Jul 20 04:54:26 2012	76%
MLE IBD:	Fri Jul 20 04:54:53 2012	83%
MLE IBD:	Fri Jul 20 04:55:14 2012	90%
MLE IBD:	Fri Jul 20 04:55:39 2012	97%
MLE IBD:	Fri Jul 20 04:55:45 2012	100%

```

> ibd.coeff <- snpgdsIBDSelection(ibd)

> plot(ibd.coeff$k0, ibd.coeff$k1, xlim=c(0,1), ylim=c(0,1),
+       xlab="k0", ylab="k1", main="YRI samples (MLE)")
> lines(c(0,1), c(1,0), col="red", lty=2)

```



### 3.4 Identity-By-State Analysis

For the  $n$  individuals in a sample, **snpgdsIBS** can be used to create a  $n \times n$  matrix of genome-wide average IBS pairwise identities:

```
> ibs <- snpgdsIBS(genofile, num.thread=2)
```

Identity-By-State (IBS) analysis on SNP genotypes:

Removing 365 non-autosomal SNPs

Removing 1 SNPs (monomorphic, < MAF, or > missing rate)

Working space: 279 samples, 8722 SNPs

Using 2 CPU cores.

IBS: the sum of all working genotypes = 2446510

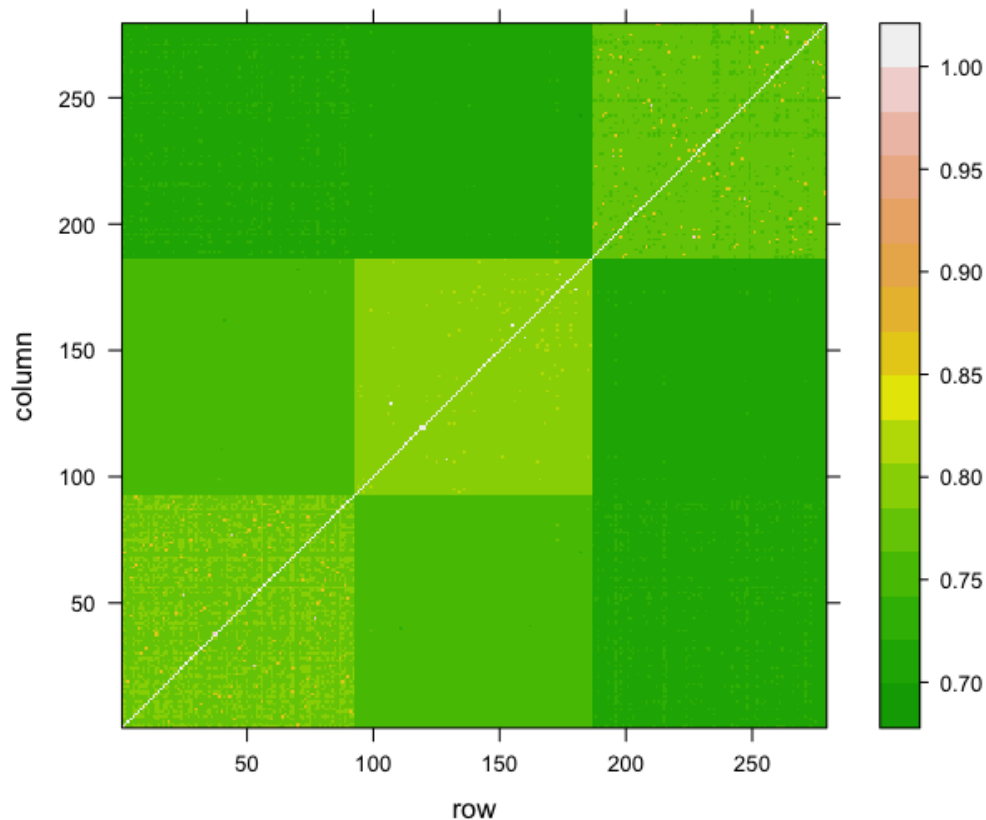
IBS: Fri Jul 20 04:55:47 2012 0%

IBS: Fri Jul 20 04:55:48 2012 100%

```
> pop <- read.gdsn(index.gdsn(genofile, c("sample.annot", "pop.group")))
```

The heat map is shown:

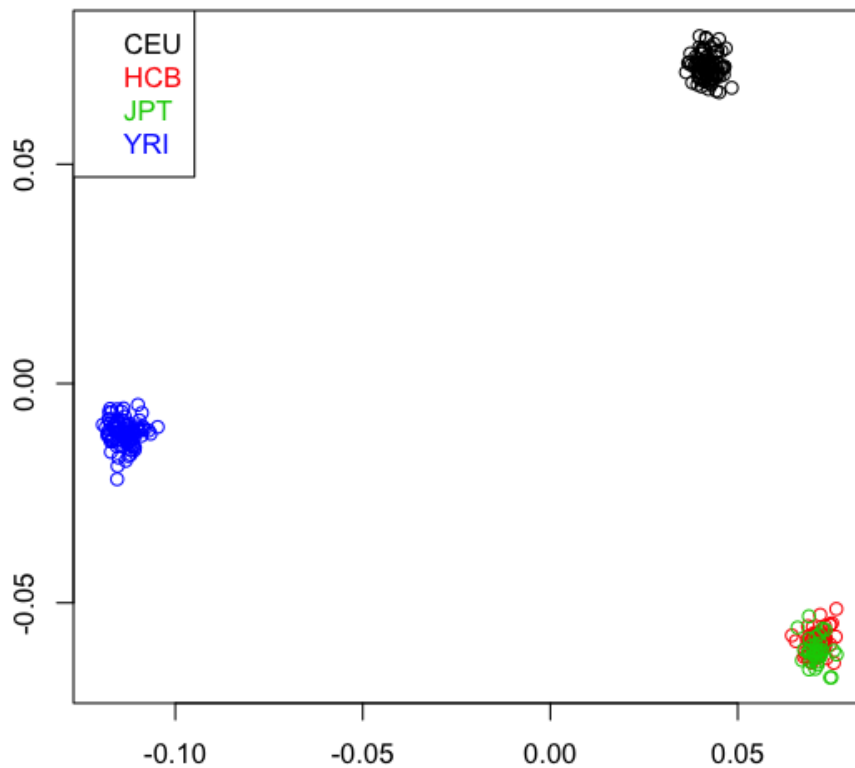
```
> library(lattice)
> L <- order(pop)
> levelplot(ibs$ibs[L, L], col.regions = terrain.colors)
```



To perform multidimensional scaling analysis on the  $n \times n$  matrix of genome-wide IBS pairwise distances:

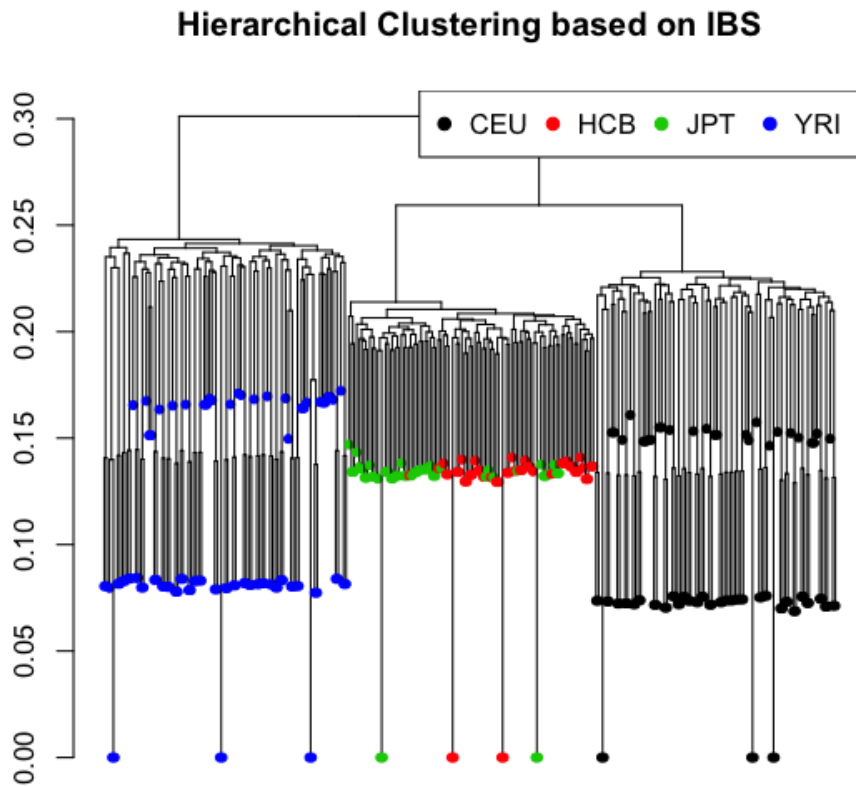
```
> loc <- cmdscale(1 - ibs$ibs, k = 2)
> x <- loc[, 1]; y <- loc[, 2]
> race <- as.factor(pop)
> plot(x, y, col=race, xlab = "", ylab = "",
+      main = "Multidimensional Scaling Analysis (IBS Distance)")
> legend("topleft", legend=levels(race), text.col=1:nlevels(race))
```

## Multidimensional Scaling Analysis (IBS Distance)



To perform cluster analysis on the  $n \times n$  matrix of genome-wide IBS pairwise distances:

```
> d <- 1 - ibs$ibs
> colnames(d) <- rownames(d) <- pop
> hc <- hclust(as.dist(d))
> obj <- as.dendrogram(hc, hang=0.2)
> add.point <- function(n, group) {
+   if (is.leaf(n))
+   {
+     attr(n, "nodePar") <- list(pch=20, col=match(attr(n, "label"), group))
+   }
+   n
+ }
> obj <- dendrapply(obj, add.point, group=levels(race))
> plot(obj, leaflab="none", main="Hierarchical Clustering based on IBS")
> legend("topright", legend=levels(race), col=1:nlevels(race), pch=19, ncol=4)
```



```
> # close the GDS file
> closefn.gds(genofile)
```

## 4 Resources

1. CoreArray project: <http://corearray.sourceforge.net/>
2. gdsfmt R package: <http://cran.r-project.org/web/packages/gdsfmt/index.html>
3. SNPRelate R package: <http://cran.r-project.org/web/packages/SNPRelate/index.html>

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